



K25U 2953

Reg. No. : .....

Name : .....

III Semester B.Sc. Degree (CBCSS – OBE – Supplementary/Improvement)  
Examination, November 2025  
(2019 to 2023 Admissions)

COMPLEMENTARY ELECTIVE COURSE IN STATISTICS FOR B.SC.  
GEOGRAPHY/PSYCHOLOGY

3C 03 STA (G&P) : Probability and Distribution Theory

Time : 3 Hours

Max. Marks : 40

**Instruction :** Use of calculators and statistical tables are **permitted**.

PART – A  
(Short Answer)

Answer **all 6** questions.

(6×1= 6)

1. Give the classical definition of probability.
2. Define disjoint events.
3. Can two mutually exclusive be independent ?
4. Write down the pdf of a normal distribution with mean 0 and variance 4.
5. A Poisson distribution has mean 2. Write down its pmf.
6. A binomial distribution has mean 4 and variance  $\frac{4}{3}$ . Find  $P(X = 0)$ .

PART – B  
(Short Essay)

Answer **any 6** questions.

(6×2=12)

7. State multiplication theorem in probability for any two events. Deduce it when the events are independent.
8. State Baye's theorem.

P.T.O.



9. Define pdf of a continuous random variable. What are its properties ?
10. A discrete random variable  $X$  takes values  $-2, -1, 1, 2$  each with probability  $0.25$ . Find the expected value of  $2X$ .
11. Give any two properties of binomial distribution.
12. If  $X$  is a random variable following Poisson distribution such that  $P(X = 1) = P(X = 2)$ . Find  $P(X = 0)$ .
13. Give the properties of normal distribution.
14. Give the pdf of a chi square distribution with 2 degree of freedom.

**PART – C**  
**(Essay)**

Answer **any 4** questions.

**(4×3=12)**

15. State and prove addition theorem in probability for any two events.
16. Define a random variable. Discuss different types of random variables with suitable examples.
17. Check whether the function given by  $f(x) = \frac{x}{21}, x = 1, 2, 3, 4, 5, 6$  is a pmf. If it is a pmf, obtain the mean.
18. Give the pdf of exponential distribution. Obtain its distribution function.
19. Obtain the mean of Poisson distribution.
20. Define  $t$  distribution and state its properties.

**PART – D**  
**(Long Essay)**

Answer **any 2** questions.

**(2×5=10)**

21. Three identical boxes contain respectively 4 white and 3 red balls; 3 white and 7 red balls; 2 white and 3 red balls. A box is chosen at random and a ball is drawn out of it. If the ball is found to be white, what is the probability that second box was selected ?



22. Let  $X$  discrete random variable with  $P(X = 0) = 0.25$ ,  $P(X = 1) = 0.125$ ,  $P(X = 2) = 0.125$  and  $P(X = 3) = 0.5$ . Graph the pmf and cdf of  $X$ .
23. A machine in a factory produces components continuously. Each day a sample of 20 components are selected and tested. Over a period of 30 days the number of defective components in the sample is recorded as follows. Fit a Poisson distribution and calculate expected frequencies.

No. of defectives per sample	0	1	2	3	4	5
No. of Samples	9	9	7	3	2	0

24. If  $X_1, X_2, X_3$  be a random sample from  $N(0, \sigma^2)$ , what is the distribution of  $\frac{x_1^2 + x_2^2 + x_3^2}{\sigma^2}$ ? State the sampling distribution of the statistics  $\frac{\sqrt{2}x_1}{\sqrt{x_2^2 + x_3^2}}$  and  $\frac{x_1^2}{x_2^2}$ .

